

## Exercise 1

Characterize the set of all invalid UTF-8 multi-byte sequences. If you think about it, this boils down to saying which bytes cannot occur as the first byte in a UTF-8 multi-byte sequence, and which bytes cannot occur as a second / third / fourth byte in a UTF-8 multi-byte sequence. You should of course justify your answer and not just claim things.

## Exercise 2

Write the following program in either Java or C++. Generate a random sequence of $n$ bytes, where $n$ is an input parameter. Then go over the string, and using your characterization from Exercise 1, replace as few characters as possible such that the resulting string is completely valid UTF-8. Make an effort to write efficient code. In any case, your program should run in $O(n)$ time. (Note: "as few characters as possible" is not meant in a mathematical optimal sense, it's just so you avoid extremes like replacing all characters with ASCII code $\geq 128$ by zero.)

## Exercise 3

If you wrote the program for Exercise 1 in Java, now write the same program in C++. If you wrote it in C++, now write it in Java. Again, make an effort to write efficient code.

## Exercise 4

Write the program from Exercise 1 in a script language. You may choose between Perl, Python, and PHP. Again, make an effort to write efficient code.

## Exercise 5

Run all three programs for $n=10^{3}, 10^{6}, 10^{9}$. Measure the running time for each program and each setting of $n$, averaged over 10 runs in each case. Measure only the time for the actual string repair, not the time for generating the random sequence. Summarize your results in a table with 3 columns (one for each programming language) and 3 rows (one for each setting of $n$ ). Briefly discuss your results.

