

Exercise Sheet 9 — Solutions

Exercise 1

Here is an algorithm that decides whether the UTF-8 multi-byte sequence starting at a given position in a string is valid or not:

1. If the first byte is of the form `0xxxxxxx`, the sequence is *valid* (all ASCII codes < 128 are valid UTF-8 codes).
2. If the first byte is of the form `10xxxxxx` or `11111xxx`, the sequence is invalid (the first byte must start with 0, 110, 1110, or 11110).
3. If the first byte is of the form `1100000x`, the sequence is invalid (2-byte UTF-8 sequence with code point < 128).
4. If the first byte is `11100000` and the second byte is of the form `100xxxxx`, the sequence is invalid (3-byte sequence with code point < 2048).
5. If the first byte is `11110000` and the second byte is of the form `1000xxxx`, the sequence is invalid (4-byte sequence with code point < 65536).
6. If the number of leading 1s before the first 0 is m , and one of the next $m - 1$ bytes is not of the form `10xxxxxx`, the sequence is invalid (all bytes after the first must start with 10).
7. All other sequences are valid.

Exercise 2

Here is a C++ implementation that implements the characterization from above in the most straightforward way (by Hannah).

```
#include <stdlib.h>
#include <stdio.h>
#include <time.h>
int main(int argc, char** argv)
{
    unsigned int n = argc > 1 ? atoi(argv[1]) : 1000000;
    // Leave some space so that we don't have to check boundary conditions below.
    unsigned char* s = new unsigned char[n+3];
    for (int i = 0; i < n; ++i) s[i] = (unsigned char)(256 * drand48());
    clock_t t = clock();
    int i = 0;
```

```

while (i < n)
{
    // Count the number of leading 1s in the first byte.
    int l = s[i] < 128 ? 0 : (s[i] < 192 ? 1 : (s[i] < 224 ? 2 : (s[i] < 240 ? 3 : (s[i] < 248 ? 4 : 5)))
    // Should be 0, 2, 3, or 4, otherwise invalid first byte.
    if (l == 1 || l == 5) { s[i++] = 0; continue; }
    // Make sure that the next l - 1 bytes all start with 10.
    for (int j = i + 1; j < i + l; ++j) s[j] = s[j] & 63 + 128 ;
    // First byte must not be 1100000x.
    if (s[i] & 254 == 192) { s[i++] = 0; continue; }
    // First two bytes must not be 11100000 100xxxxx.
    if (s[i] == 224 && s[i+1] & 224 == 128) { s[i] = s[i+1] = 0; i += 2; continue; }
    // First two bytes must not be 11110000 1000xxxx.
    if (s[i] == 240 && s[i+1] & 240 == 128) { s[i] = s[i+1] = s[i+2] = 0; i += 3; continue; }
}
printf("Corrected random %d-byte string in %.2f seconds\n", n, (double)(clock() - t)/CLOCKS_PER_SEC);
}

```

Exercise 3

Here is Marjan's solution for JAVA.

```

import java.util.*;
public class Ex9
{
    public static void main(String[] args) {
        int n = Integer.parseInt(args[0]);
        char[] seq = new char[n];
        Random rand = new Random();
        for(int i = 0; i < n; i++)
            seq[i] = (char)(1 + rand.nextInt(255));
        long startTime = System.nanoTime();
        for(int i = 0; i < n; i++) {
            if (seq[i] > 127 && seq[i] < 224) { // start of a 2-byte UTF-8 sequence
                if (seq[i] < 194) { // invalid first byte
                    seq[i] = '0';
                    if (i < n - 1)
                        if (seq[i+1] > 127) seq[i+1] = '0';
                }
            }
            else { // first byte ok
                if (i < n - 1)
                    seq[i] = '0';
            }
            else
                if (seq[i+1] < 128) { // invalid second byte
                    seq[i+1] = '0'; seq[i] = '0';
                }
        }
    }
}

```

```

    }
}
else
if (seq[i] >= 224 && seq[i] < 240) { // start of a 3-byte UTF-8 sequence
    if (i < n - 1) {
        if (seq[i+1] < 160 || seq[i+1] > 191) { // invalid second byte
            seq[i] = '0'; seq[i+1] = '0';
            if (i < n - 2) // is there a third byte?
                if (seq[i+2] > 127)
                    seq[i+2] = '0';
        }
        else { // second byte ok
            if (i < n - 2) // is there a third byte?
                if (seq[i+2] < 128 || seq[i+2] > 191) { // invalid third byte
                    seq[i] = '0'; seq[i+1] = '0'; seq[i+2] = '0';
                }
            else { // no third byte!
                seq[i] = '0'; seq[i+1] = '0';
            }
        }
    }
}
else // no second byte
    seq[i] = '0';
}
else
if (seq[i] >= 240) { // 4-byte UTF-8 sequence
    if (i == n - 1)
        seq[i] = '0';
    else
        if (i == n - 2) { seq[i] = '0'; seq[i+1] = '0'; }
        else
            if (i == n - 3) { seq[i] = '0'; seq[i+1] = '0'; seq[i+2] = '0'; }
            else
                if (i == n - 4) {
                    seq[i] = '0'; seq[i+1] = '0'; seq[i+2] = '0'; seq[i+3] = '0';
                }
                else {
                    if (seq[i+1] < 144 || seq[i+1] > 191) { // invalid second
                        seq[i] = '0'; seq[i+1] = '0';
                        if (seq[i+2] > 127) {
                            seq[i+2] = '0';
                            if (seq[i+3] > 127) seq[i+3] = '0';
                        }
                    }
                    else { // second byte ok
                        if (seq[i+2] < 128 || seq[i+2] > 191) { // invalid third
                            seq[i] = '0'; seq[i+1] = '0'; seq[i+2] = '0';
                        }
                    }
                }
            }
        }
    }
}

```

```

        if (seq[i+3] > 127) seq[i+3] = '0';
    }
    else { // third byte ok
        if (seq[i+3] < 128 || seq[i+3] > 191) { // invalid fourth
            seq[i] = '0'; seq[i+1] = '0'; seq[i+2] = '0'; seq[i+3] = '0';
        }
    }
}
}
}

long stopTime = System.nanoTime() - startTime;
System.out.println(" done. " + stopTime / 1000 + " usec.");
}
}

```

Exercise 4

Here is Marjan's solution for Perl.

```

#!/usr/bin/perl/
use Time::HiRes;
use warnings;
$n = $ARGV[0];
@seq=();
for($i = 0; $i < $n; $i++)
{
    $seq[$i] = 1 + int(rand(255));
}
$start = [Time::HiRes::gettimeofday()];
for($i = 0; $i < $n; $i++)
{
    if ($seq[$i] > 127 && $seq[$i] < 224) { # start of a 2-byte UTF-8 $sequence
        if ($seq[$i] < 194) { # invalid first bytepr1
            $seq[$i] = 0;
            if ($i < $n - 1)
            {
                if ($seq[$i+1] > 127) {
                    $seq[$i+1] = 0;
                }
            }
        }
        else # first byte ok
        {
            if ($i < $n - 1) {
                $seq[$i] = 0;
            }
        }
    }
}

```

```

    }
    else {
        if ($seq[$i+1] < 128) { # invalid second byte
            $seq[$i+1] = 0; $seq[$i] = 0;
        }
    }
}
}
else {
    if ($seq[$i] >= 224 && $seq[$i] < 240) { # start of a 3-byte UTF-8 $seq
        if ($i < $n - 1) {
            if ($seq[$i+1] < 160 || $seq[$i+1] > 191) { # invalid second byte
                $seq[$i] = 0; $seq[$i+1] = 0;
                if ($i < $n - 2) { # is there a third byte?
                    if ($seq[$i+2] > 127) {
                        $seq[$i+2] = 0;
                    }
                }
            }
        }
        else { # second byte ok
            if ($i < $n - 2) { # is there a third byte?
                if ($seq[$i+2] < 128 || $seq[$i+2] > 191) { # invalid third byte
                    $seq[$i] = 0; $seq[$i+1] = 0; $seq[$i+2] = 0;
                }
            }
            else { # no third byte!
                $seq[$i] = 0; $seq[$i+1] = 0;
            }
        }
    }
    else { # no second byte
        $seq[$i] = 0;
    }
}
else {
    if ($seq[$i] >= 240) { # 4-byte UTF-8 $sequence
        if ($i == $n - 1) { $seq[$i] = 0; }
        else {
            if ($i == $n - 2) { $seq[$i] = 0; $seq[$i+1] = 0; }
            else {
                if ($i == $n - 3) {
                    $seq[$i] = 0; $seq[$i+1] = 0; $seq[$i+2] = 0;
                }
                else {
                    if ($i == $n - 4) {
                        $seq[$i] = 0; $seq[$i+1] = 0; $seq[$i+2] = 0; $seq[$i+3] = 0;
                    }
                }
            }
        }
    }
}

```


faster than interpreted programming languages like Perl (here almost two orders of magnitude or 100 times faster). As for JAVA and C++, it is generally accepted that C++ compilers perform generally faster than JAVA (not much faster though, and not all C++ compilers). In our own example, C++ performs significantly faster than JAVA only when the size of the input is small, with very small difference for very large input.